

## Address Allocation Models



## Clean Slate Research “Agenda”

R. Guerin  
University of Pennsylvania

1

## Some Level Setting

- What does “clean slate research” have to do with allocation of IP addresses?
  - Learn from past mistakes and try to avoid repeating them
  - Identify existing weaknesses and figure out how to exploit them to displace IP
  - As a matter of fact the IPv6 vs. IPv4 story holds many lessons that clean slate proposals can benefit from
- Any clean slate proposal will have to
  - Articulate its value over the incumbent technology
  - Evaluate the need for and trade-off associated with gateways
  - Set its price so as to be competitive
  - Understand the dynamics and ultimate targets (equilibrium points) of technology migration

2

## Truth in Advertising

- I don't claim to
  - Be an expert in clean slate proposals (no crystal ball, yet!)
  - Understand all/any of the issues associated with allocation of addresses, be they IPv4 or IPv6
  - Have a specific proposal for allocating new IPv6 addresses or the remaining IPv4 addresses
  - Understand the many ways in which address allocation can affect network neutrality
- I will attempt to
  - Outline a FIND (clean slate) project whose motivations may be relevant to the issue of address allocation
    - *"On the Economic Viability of Network Architectures"* – R. Guerin and K. Hosanagar (U. Penn.) and A. Odlyzko and Z.-L. Zhang (U. Minn.)
  - Present some initial findings that illustrate the kind of issues one may face when dealing with IPv4 and IPv6 address allocation
    - *"Dynamics of technology diffusion in the presence of network externalities"* – Joint work with K. Hosanagar, Y. Jin, A. Odlyzko, S. Sen and Z.-L. Zhang

3

## Project Motivations

- Success of new technologies depends not only on their technical advantages, but also on economic factors
  - Many technologies have failed to widely deploy
  - Ex: IPv6, various QoS services
- How do we assess (design?) new network architectures that are not only technically superior but also economically viable?

4  
4

## Grand Objectives

- Identify key economic factors that influence design choices and trade-offs in developing, deploying and evolving network architectures
- Model the functional relationships between the economic factors and new technologies in network architecture designs
- Compare alternative network architectures in terms of their economic viability

5  
5

## Actual Research Topics

- ☞ Identify the impact of incumbent technology on new network architecture adoption
  - Model the dynamics of technology adoption in a network setting
- Quantify the trade-off between diversity and integration in network offerings
  - Many services over a single network vs.
  - Many services over separate multiple networks and the impact of virtualization on those choices
- Assess the benefits of open and flexible network architectures

6  
6

## Parameters of Interest

- Intrinsic benefits of an architecture/technology
- Network externalities
  - From users of the same technology
  - Across technologies when converters/gateways are available
- Costs
  - Fixed cost: deployment cost
  - Variable cost: operation and maintenance cost
  - Switching costs (getting to learn a new technology)
  - How they vary over time (learning curve) and as a function of technology complexity
- Pricing
  - Initial settings and dynamic strategies
- Many if not all of these apply equally to IPv4→IPv6 migration

7

## Our Focus and Initial Goals

- Develop a quantitative understanding of what can happen (dynamics and possible equilibria) when introducing a new network technology aimed at displacing an incumbent
  - And yes, that means models
- Identify possible outcomes and the parameters affecting them
  - How many equilibria, are they stable or not?
  - Effect of incumbent market penetration
  - Need for seeding of new technology
  - Sensitivity to initial pricing
  - Dynamics of technology adoption
  - When do technologies coexist vs. having one dominate?
- Non Goals
  - Not seeking “recipes” that can be readily applied to predict the outcome for specific technology configurations, e.g., IPv6 at \$2/address wipes out IPv4 but at \$5/address it never takes off...

8

## First Step

- What does it take to displace a (strong) incumbent (IPv4) with a new, niftier (clean slate or IPv6) technology
  - Each technology delivers a certain intrinsic utility ( $q_i$ ,  $i=1,2$ ) with presumably  $q_1 \leq q_2$ , and charges a certain price ( $p_i$ ,  $i=1,2$ )
    - All these are **generic** quantities with a common unit (no attempt – yet – at “dollarizing” these quantities)
  - Users have individual preferences ( $\theta$ ) that shape their technology adoption behavior
    - User preferences have a certain (known) distribution, e.g., uniform
  - Technology 1 enjoys an existing market penetration when technology 2 is first introduced at time  $t=0$  ( $x_1(0)>0$ ,  $x_2(0)=0$ )
    - Network externalities increase utility of each technology in “proportion” to its number of adopters
- Model should capture the dynamics of technology adoption in this scenario
  - Identification of (stable) equilibrium points
  - Trajectory of equilibrium
  - More importantly, we should extract a better understanding/insight of what can happen and the key parameters affecting the outcome

9

## Basic Notation

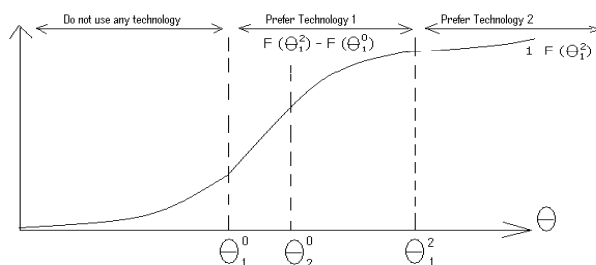
- Basic parameters
  - $x_i$ : fraction of technology  $i$  adopters ( $0 \leq x_i \leq 1$ ,  $i=1,2$ ;  $x_1 + x_2 \leq 1$ )
  - $\theta$ : individual user preference (uniformly distributed in  $[0,1]$ )
  - $q_i$ : utility of technology  $i$
  - $v(x_i)$ : network externality (assume  $v(x_i)=x_i$ )
  - $p_i$ : price of technology  $i$ ,  $i=1,2$
- Utility of technology  $i$ :  $U_i(\theta, x_i) = \theta q_i + x_i - p_i$ ,  $i=1,2$
- User behavior (rational decision)
 

{	no technology	if	$U_i < 0$	for $i = 1,2$
	technology 1	if	$U_1 > 0$	and $U_1 > U_2$
	technology 2	if	$U_2 > 0$	and $U_2 > U_1$

10

## Technology Adoption Model

- Indifference points for technology adoption
  - $\theta_1^0 : U_1(\theta) \geq 0$  if  $\theta \geq \theta_1^0$ , users adopt technology 1
  - $\theta_2^0 : U_2(\theta) \geq 0$  if  $\theta \geq \theta_2^0$ , users adopt technology 2
  - $\theta_1^2 : U_2(\theta) \geq U_1(\theta)$  if  $\theta \geq \theta_1^2$ , users prefer technology 2
- Sample outcome

11  
11

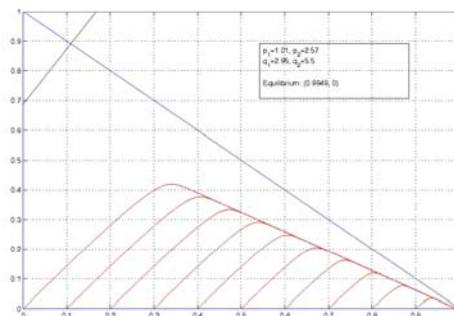
## Technology Diffusion

- Let  $H_i(\underline{x})$ ,  $i=1,2$  and  $\underline{x}=(x_1, x_2)$  denote the “measure” of the set of adopters of technology  $i$  (how many users have adopted it)
  - At equilibrium, we must have  $H_i(\underline{x}^*)=x_i^*$ ,  $i=1,2$
- Diffusion of technology proceeds iteratively
  - In each interval of duration  $\Delta t$ ,  $x_i(t+\Delta t)=H_i(\underline{x}(t))$
  - This can be used to define a differential equation
- Solution identifies different “regions” of the parameter space  $(p_1, q_1, p_2, q_2)$ 
  - In each region we can
    - Characterize and validate candidate equilibrium points and determine if they are stable or unstable
    - Solve the differential equation to identify the trajectory of technology diffusion
- Most importantly, use this machinery to gain some insight into possible behaviors of technology competition
  - Some representative examples to follow

12  
12

## The Impact of Pricing – (1a)

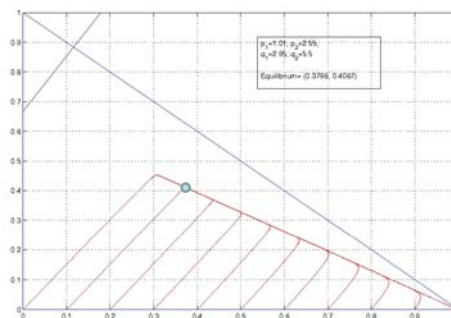
- Two technologies
  - $q_1 = 2.95, p_1 = 1.01$
  - $q_2 = 5.5, p_2 = 2.57$
- Technology 2 prices itself out of (eventual) existence
  - Note that it does take off and gain some traction, but technology 1 is still growing faster and eventually wins
  - Outcome is *independent* of initial technology 1 penetration



13

## The Impact of Pricing – (1b)

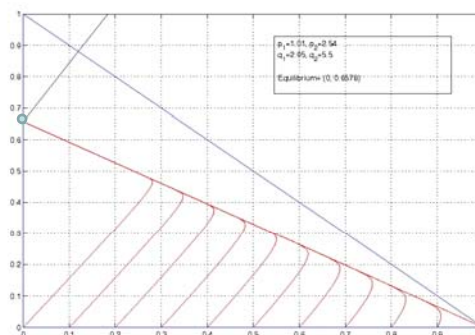
- Two technologies
  - $q_1 = 2.95, p_1 = 1.01$
  - $q_2 = 5.5, p_2 = 2.55$
- Technology 2 prices itself competitively
  - The two technologies converge to unhappy coexistence (roughly equal market shares)
  - Outcome is again *independent* of initial technology 1 penetration



14

## The Impact of Pricing – (1c)

- Two technologies
  - $q_1 = 2.95, p_1 = 1.01$
  - $q_2 = 5.5, p_2 = 2.54$
- Technology 2 prices itself to win
  - Technology 1 continues growing for some time after the introduction of technology 2, but is eventually wiped out
  - Outcome is again *independent* of initial technology 1 penetration



15

## Taking Stock – (1)

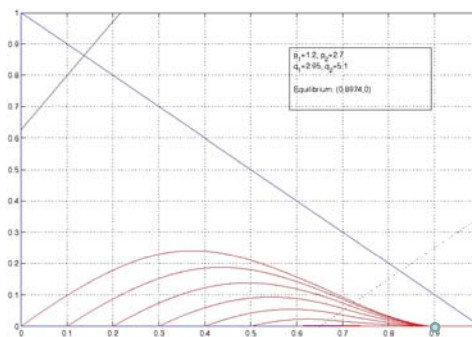
- A better technology does not always win
  - No surprise there
- A full range of possible outcomes
  - Either or both technology can survive
- Rapid transitions between different outcomes based on small price changes
  - $p_2 = 2.54$ : only technology 1 survives
  - $p_2 = 2.55$ : both technologies survive
  - $p_2 = 2.57$ : only technology 2 survives
- The initial penetration of technology 1 did not affect the outcome
- Are these general conclusions or can we see different behaviors?

16



## The Impact of Pricing – (2a)

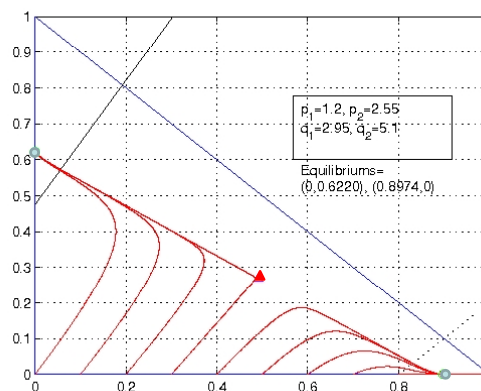
- Two technologies
  - $q_1 = 2.95, p_1 = 1.2$  (higher)
  - $q_2 = 5.1, p_2 = 2.7$
- Technology 2 again prices itself out of (eventual) existence
  - As before, it takes off, but grows more slowly than technology 1 which eventually wins
  - Outcome still *independent* of the initial penetration of technology 1



17

## The Impact of Pricing – (2b)

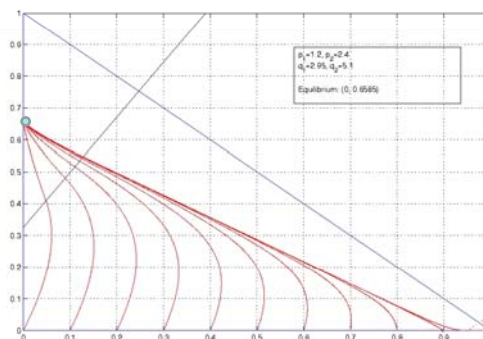
- Two technologies
  - $q_1 = 2.95, p_1 = 1.2$  (higher)
  - $q_2 = 5.1, p_2 = 2.55$
- The outcome now depends on the initial penetration of technology 1
  - Above a certain threshold ( $\sim 0.4$ ), it eventually prevails
  - Below the threshold, only technology 2 survives in spite of continued robust growth of technology 1 after technology 2 is first introduced
  - Note the presence of an *unstable* equilibrium  $\blacktriangle$  where both technologies would have survived



18

## The Impact of Pricing – (2c)

- Two technologies
  - $q_1 = 2.95, p_1 = 1.2$  (higher)
  - $q_2 = 5.1, p_2 = 2.4$
- As in scenario 1, technology 2 now prices itself to be the only one to survive
  - Technology 1 continues to grow (slowly) for some time after the introduction of technology 2, but is eventually wiped out
  - Outcome is back to being *independent* of initial technology 1 penetration



19

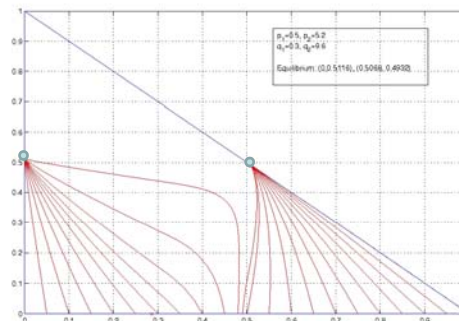
## Taking Stock – (2)

- We have now seen scenarios where both pricing and the initial penetration of the incumbent play a role
  - Technology 1 was the same as before, just a bit more expensive
  - Technology 2 was slightly less performant than in the previous examples
- Basically we went, using two mostly similar configurations, from an environment with a stable equilibrium where both technology co-existed to one where only one of the two technologies survived

20

## One Last Example – (3a)

- Two technologies
  - $q_1=0.3, p_1=0.5$
  - $q_2=9.6, p_2=5.2$
- We now have a low-quality but cheap technology competing against a high-quality but expensive one
- The outcome depends on the initial penetration of the cheaper technology
  - Above a threshold, both technologies end-up coexisting and achieve full market penetration
  - Below the threshold only the better technology survives



21

## What Is Missing? Lots of Things

- Time-varying technology quality and price
  - It gets better and cheaper over time
- Pricing that depends on the number of adopters
  - The more people are using the technology the cheaper it gets
- Profit model and profit maximization strategies
  - How to charge to maximize profit over a certain time period
- Dynamic pricing strategies
  - How does each technology react to maximize its chances of survival and/or its profit
- Addition of gateways that deliver cross-technology externalities
- Validation
  - Identify existing/ongoing deployment scenarios on which to try to apply this, i.e., examples of prices, costs, qualities, etc.
  - And yes that means that we need more DATA!
- And the list goes on...

22

## Conclusion

- Interactions of competing technologies with network externalities can give rise to a wide range of outcomes based on
  - Pricing, technology quality, level of penetration of the incumbent, etc.
- We are starting to develop some basic models to explore these complex interactions
  - Much work remains, but the end-result should offer improved insight of what to watch for or take into account when assessing how to best introduce new network technologies
- And yes, this might be applicable to IPv4-IPv6 migration

23